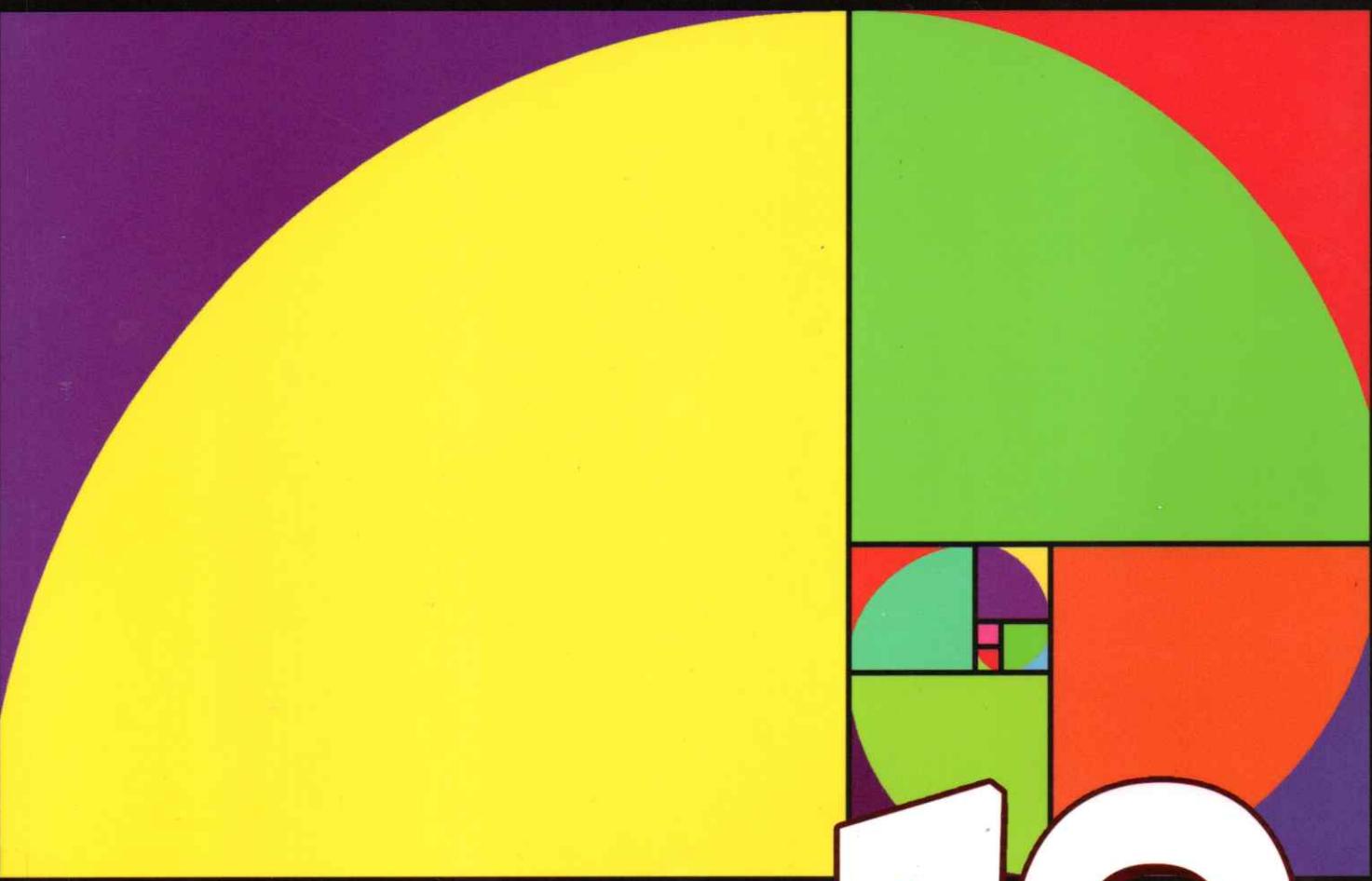




# E-Math

Worktext in Mathematics



Orlando A. Oronce

Marilyn O. Mendoza

Authors

# 10

Revised Edition

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**Orlando A. Oronce  
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## Authors

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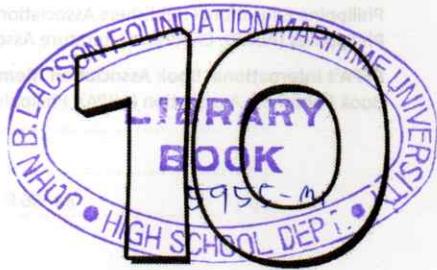
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• Interactive Mathematics I–IV  
• Journal  
• Math Probe I–IV  
• Workbook  
• Workbook in Mathematics I–IV

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