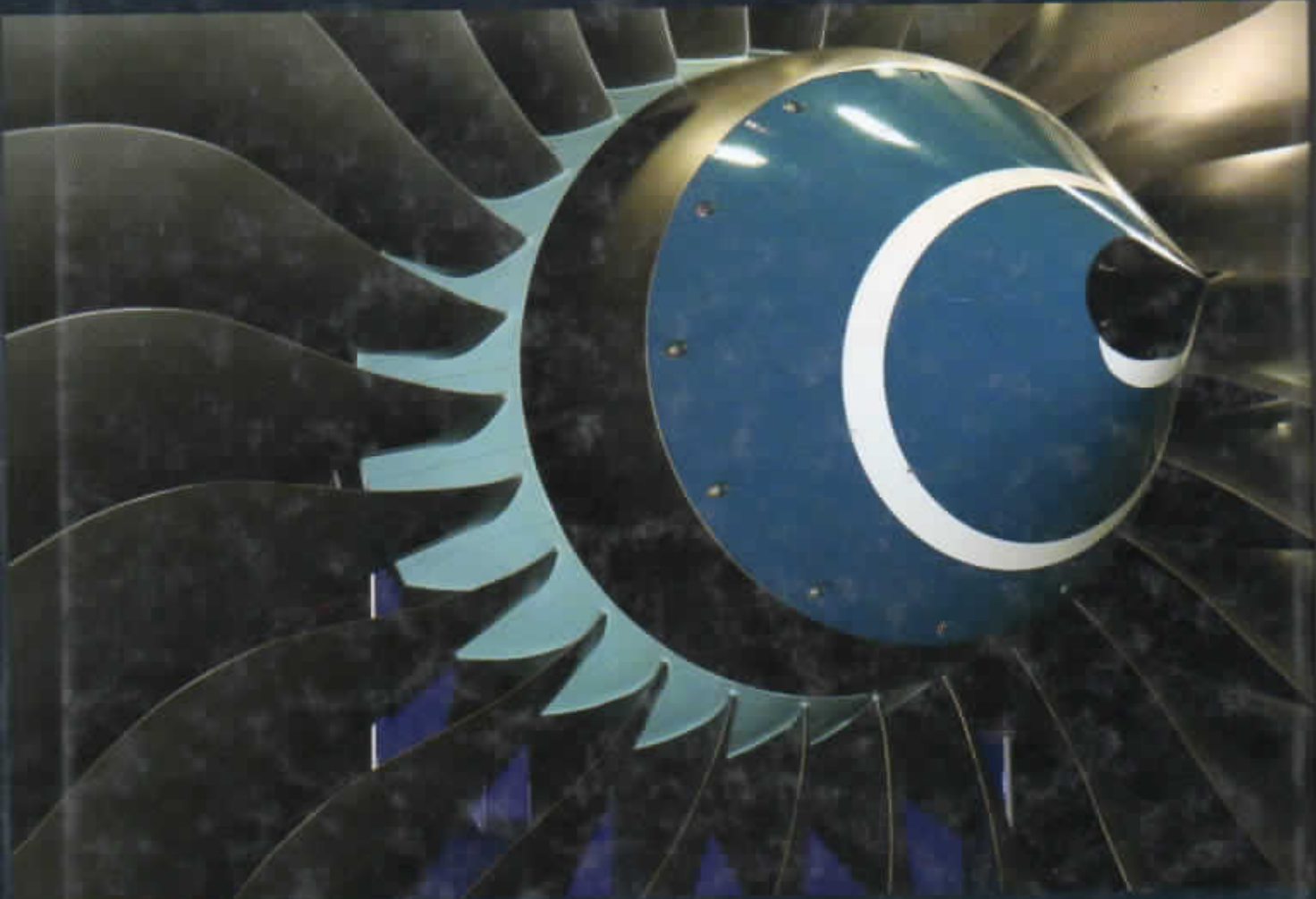


# Fluid Mechanics and Thermodynamics of Turbomachinery



S. L. DIXON AND C. A. HALL

SEVENTH EDITION



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Seventh Edition

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# Contents

Preface to the Seventh Edition .....	xi
Acknowledgments .....	xiii
List of Symbols.....	xv
<b>CHAPTER 1 Introduction: Basic Principles.....</b>	<b>1</b>
1.1 Definition of a turbomachine .....	1
1.2 Coordinate system .....	2
1.3 The fundamental laws .....	6
1.4 The equation of continuity .....	6
1.5 The first law of thermodynamics .....	7
1.6 The momentum equation.....	9
1.7 The second law of thermodynamics—entropy .....	11
1.8 Bernoulli's equation .....	13
1.9 The thermodynamic properties of fluids.....	14
1.10 Compressible flow relations for perfect gases.....	18
1.11 Definitions of efficiency .....	22
1.12 Small stage or polytropic efficiency.....	27
1.13 The inherent unsteadiness of the flow within turbomachines.....	33
References .....	36
<b>CHAPTER 2 Dimensional Analysis: Similitude .....</b>	<b>39</b>
2.1 Dimensional analysis and performance laws.....	39
2.2 Incompressible fluid analysis.....	40
2.3 Performance characteristics for low-speed machines.....	42
2.4 Compressible flow analysis.....	44
2.5 Performance characteristics for high-speed machines.....	48
2.6 Specific speed and specific diameter.....	53
2.7 Cavitation.....	61
References .....	66
<b>CHAPTER 3 Two-Dimensional Cascades .....</b>	<b>69</b>
3.1 Introduction .....	69
3.2 Cascade geometry.....	72
3.3 Cascade flow characteristics .....	75
3.4 Analysis of cascade forces .....	80
3.5 Compressor cascade performance .....	84
3.6 Turbine cascades .....	94
3.7 Cascade computational analysis.....	108
References .....	115

<b>CHAPTER 4</b>	<b>Axial-Flow Turbines: Mean-Line Analysis and Design</b>	119
4.1	Introduction	119
4.2	Velocity diagrams of the axial turbine stage	121
4.3	Turbine stage design parameters	122
4.4	Thermodynamics of the axial turbine stage	123
4.5	Repeating stage turbines	124
4.6	Stage losses and efficiency	127
4.7	Preliminary axial turbine design	133
4.8	Styles of turbine	135
4.9	Effect of reaction on efficiency	140
4.10	Diffusion within blade rows	141
4.11	The efficiency correlation of Smith (1965)	143
4.12	Design point efficiency of a turbine stage	146
4.13	Stresses in turbine rotor blades	150
4.14	Turbine blade cooling	155
4.15	Turbine flow characteristics	159
	References	166
<b>CHAPTER 5</b>	<b>Axial-Flow Compressors and Ducted Fans</b>	169
5.1	Introduction	169
5.2	Mean-line analysis of the compressor stage	170
5.3	Velocity diagrams of the compressor stage	171
5.4	Thermodynamics of the compressor stage	172
5.5	Stage loss relationships and efficiency	173
5.6	Mean-line calculation through a compressor rotor	176
5.7	Preliminary compressor stage design	180
5.8	Off-design performance	187
5.9	Multistage compressor performance	188
5.10	High Mach number compressor stages	195
5.11	Stall and surge phenomena in compressors	198
5.12	Low speed ducted fans	204
	References	213
<b>CHAPTER 6</b>	<b>Three-Dimensional Flows in Axial Turbomachines</b>	215
6.1	Introduction	215
6.2	Theory of radial equilibrium	215
6.3	The indirect problem	218
6.4	The direct problem	227
6.5	Compressible flow through a fixed blade row	229
6.6	Constant specific mass flow	230
6.7	Off-design performance of a stage	232
6.8	Free-vortex turbine stage	233
6.9	Actuator disc approach	235

6.10	Computational through-flow methods .....	242
6.11	3D flow features .....	245
6.12	3D design .....	250
6.13	The application of 3D computational fluid dynamics .....	252
	References .....	262
<b>CHAPTER 7</b>	<b>Centrifugal Pumps, Fans, and Compressors .....</b>	<b>265</b>
7.1	Introduction .....	265
7.2	Some definitions .....	267
7.3	Thermodynamic analysis of a centrifugal compressor .....	269
7.4	Inlet velocity limitations at the compressor eye .....	272
7.5	Design of a pump inlet .....	273
7.6	Design of a centrifugal compressor inlet .....	275
7.7	The slip factor .....	281
7.8	A unified correlation for slip factor .....	286
7.9	Head increase of a centrifugal pump .....	290
7.10	Performance of centrifugal compressors .....	292
7.11	The diffuser system .....	300
7.12	Diffuser performance parameters .....	305
7.13	Choking in a compressor stage .....	309
	References .....	316
<b>CHAPTER 8</b>	<b>Radial-Flow Gas Turbines .....</b>	<b>319</b>
8.1	Introduction .....	319
8.2	Types of IFR turbine .....	320
8.3	Thermodynamics of the 90° IFR turbine .....	322
8.4	Basic design of the rotor .....	324
8.5	Nominal design point efficiency .....	326
8.6	Some Mach number relations .....	330
8.7	The scroll and stator blades .....	331
8.8	Optimum efficiency considerations .....	334
8.9	Criterion for minimum number of blades .....	340
8.10	Design considerations for rotor exit .....	343
8.11	Significance and application of specific speed .....	348
8.12	Optimum design selection of 90° IFR turbines .....	351
8.13	Clearance and windage losses .....	352
8.14	Cooled 90° IFR turbines .....	354
	References .....	359
<b>CHAPTER 9</b>	<b>Hydraulic Turbines .....</b>	<b>361</b>
9.1	Introduction .....	361
9.2	Hydraulic turbines .....	363
9.3	The Pelton turbine .....	366

9.4	Reaction turbines.....	377
9.5	The Francis turbine.....	377
9.6	The Kaplan turbine.....	385
9.7	Effect of size on turbomachine efficiency.....	389
9.8	Cavitation in hydraulic turbines.....	391
9.9	Application of CFD to the design of hydraulic turbines.....	398
9.10	The Wells turbine.....	398
9.11	Tidal power.....	409
	References.....	417
<b>CHAPTER 10</b>	<b>Wind Turbines.....</b>	<b>419</b>
10.1	Introduction.....	419
10.2	Types of wind turbine.....	422
10.3	Performance measurement of wind turbines.....	427
10.4	Annual energy output.....	431
10.5	Statistical analysis of wind data.....	431
10.6	Actuator disc approach.....	433
10.7	Blade element theory.....	441
10.8	The BEM method.....	449
10.9	Rotor configurations.....	458
10.10	The power output at optimum conditions.....	465
10.11	HAWT blade section criteria.....	466
10.12	Developments in blade manufacture.....	467
10.13	Control methods (starting, modulating, and stopping).....	469
10.14	Blade tip shapes.....	473
10.15	Performance testing.....	474
10.16	Performance prediction codes.....	475
10.17	Environmental matters.....	478
10.18	The largest wind turbines.....	480
10.19	Final remarks.....	481
	References.....	483
	Appendix A: Preliminary Design of an Axial-Flow Turbine for a Large Turbocharger.....	487
	Appendix B: Preliminary Design of a Centrifugal Compressor for a Turbocharge.....	497
	Appendix C: Tables for the Compressible Flow of a Perfect Gas.....	507
	Appendix D: Conversion of British and American Units to SI Units.....	519
	Appendix E: Mollier Chart for Steam.....	521
	Appendix F: Answers to Problems.....	523
	Index.....	529

# Index

Note: Page numbers followed by "f" and "t" refer to figures and tables, respectively.

## A

- Actuator disc, 433–441
  - alternative proof of Betz's result, 435–436
  - approach, 235–242
  - axial flow induction factor for, 435–436, 440–441
  - axial force coefficient, 437–439
  - blade row interaction effects, 239–241
  - and boundary stream tube model, 434f
  - concept, 235, 238
  - estimating power output, 441
  - mean-value rule, 239
  - power coefficient, 436–437
  - and radial equilibrium, 238
  - settling-rate rule, 239
  - theory for compressible flow, 241–242
  - theory of, 434–435, 446–447
- Aerofoils, 73–74, 75f, 135
  - theory, 204
  - vortex system of, 442–444
  - zero lift line, 208–212
- Aileron control system, 471–473
- Ainley and Mathieson correlation, 96–98
- American units conversion to SI units, 419t–486f
- Annual energy output, 431
- Annulus wall boundary layers, 194–195
- Axial flow compressor stage, velocity diagrams for, 5–6
- Axial flow induction factor for actuator disc, 435–436, 440–441
- Axial flow turbomachine, 1, 2f
- Axial force coefficient, 437–439
- Axial velocity density ratio (AVDR), 77
- Axial-flow compressors, 169
  - blade aspect ratio, 183–186
  - casing treatment, 200–203
  - control of flow instabilities, 203
  - design of, 169
  - flow coefficient, 182
  - flow within, 169–170
  - interstage swirl, 183
  - mean-line analysis, 170–171
  - Mollier diagram for stage, 173f
  - multi-stage, 188–195
  - off-design performance, 187–188
  - reaction, 182–183
  - stage loading, 181–182
  - stage loss relationships and efficiency, 173–176
  - stall and surge in, 198–203
  - thermodynamics, 172–173
  - velocity diagrams for stage, 172f
- Axial-flow turbines, 119–121, 487
  - blade and flow angle, 494–495
  - blade aspect ratio, 492
  - blade boundary layers, loss in, 130
  - coolant flows, loss from, 131
  - design of, 122–123, 133–135, 487
  - efficiency, determining, 489–490
  - ellipse law, 159–160
  - endwall loss, 131
  - estimating pitch/chord ratio, 493–494
  - fifty percent reaction stage, 136–139
  - flow characteristics, 159–166
  - flow coefficient, 122, 126, 146f
  - flow separation loss, 130
  - mean line analysis, 119–121
  - mean radius design, 489–490
  - mean radius velocity triangles, determining, 489–490
  - mechanical arrangement, 488f
  - Mollier diagram of, 123–124, 125f, 136
  - with multiple stages, 124–125, 160–166
  - normal stage, 126
  - number of stages, 134
  - pitchline analysis, 119–120
  - reaction effect on efficiency, 140f
  - repeating stage, 124–127
  - root and tip radii, determining, 490–491
  - shock loss, 130
  - stage geometry, choosing, 492–493
  - stage loading coefficient, 123, 126, 146f
  - stage losses and efficiency, 127–133
  - stage reaction, 123, 126
  - steam turbines, 131–133
  - thermal efficiency vs. inlet gas temperature, 158f
  - thermodynamics of stage, 123–124
  - 2D loss sources, 130
  - tip leakage flows, 131
  - trailing edge mixing loss, 130
  - turbofan jet engine, 121f
  - variation of reaction at hub, 491–492
  - velocity diagrams of stage, 121–122, 136f, 137f, 149f, 160f
  - zero reaction stage, 136, 148, 149f



**B**

- Bernoulli's equation, 13–14
- Betz limit, 437
- Bioinspired technology, 478
- Blade element momentum (BEM) method, 449–457
  - parameter variation, 449–450
  - torque and axial force, evaluating, 450–453
- Blade element theory, 206–207, 441–448, 475
  - and actuator disc theory, 446–447
  - forces acting on, 444–445
  - tangential flow induction factor, 442
- Blade Mach number, 45
- Blade row method, 129
- Blade tip correction
  - performance calculations with, 456–457
  - Prandtl's method, 453–455
- Blades
  - aspect ratio, 183–186
  - cavitation coefficient, 273
  - centrifugal stresses in rotor, 151–155
  - cooling systems, 155–158
  - criterion for minimum number of, 340–343
  - developments in manufacture, 467–469
  - diffusion in, 141–143
  - element efficiency, 207–208
  - enhanced performance of, 478
  - height and mean radius, 134–135
  - loading of, 84–86
  - pitch control, 470
  - planform, 458
  - row interaction effects, 239–241
  - section criteria, 466–467
  - surface velocity distributions, 80
  - tip shapes, 473–474
  - turbine, 74–75
- "Blade-to-blade methods," 108
- British units conversion to SI units, 419*t*–486*t*

**C**

- Camber angle, 72
- Camber line, 72–75
- Cantilever IFR turbine, 320–321
- Cascades, two-dimensional, 69
  - boundary conditions, 110–111
  - calculation geometry, 108–109
  - camber angle, 72
  - circulation and lift, 83–84
  - contraction coefficient, 70
  - drag coefficient, 82–83
  - drag forces, 81–82
  - energy loss coefficient, 78

- flow characteristics, 75–80
- forces, analysis, 80–84
- geometry, 72–75
- hub–tip radius ratios, 72
- incidence effects, 87–89
- incompressible cascade analysis, 89–91
- lift coefficient, 82–83
- lift forces, 81–82
- Mach number, effects of, 92–95
- method types, 109–110
- performance parameters, 77–79
- pressure rise coefficient, 78
- profile loss coefficient, 97
- profile thickness distribution, 72
- space–chord ratio, 72
- stagger angle, 72
- stagnation pressure loss coefficient, 77
- streamtube thickness variation, 76–77
- total pressure loss coefficient, 77–78
- transonic effects, 111
- turbine loss correlations, 95–96
- viscous effects, 112–115
- wind tunnels, 70*f*
- Cavitation, 61–64
  - avoiding, 395
  - in hydraulic turbines, 391–397
  - inception, 62–63
  - limits, 62–64
  - net positive suction head, 63
  - peripheral velocity factor (PVF), 395–396
  - right turbine, selecting, 396–397
  - tensile stress in liquids, 62–63
  - vapour formation, 62
  - vapour pressure, 62–63
- Centrifugal compressor, 2*f*, 265–267
  - air mass flow, 497
  - applications of, 265
  - with backswept impeller vanes, 265–267, 266*f*, 294–297
  - blade Mach number of, 295, 297*f*
  - choking of stage, 309–316
  - design requirements, 497
  - diffuser, 268, 271–272, 310–316
  - effect of prewhirl vanes, 279–281, 280*f*
  - efficiency of impeller in, 499
  - exit stagnation pressure, 503–504
  - impeller, 268–271, 298, 310
  - impeller exit, design of, 499–500
  - impeller exit Mach number of, 295–297, 297*f*
  - impeller inlet, design of, 498–499
  - impeller radius and blade speed, 497–498
  - inlet, 309–310
  - inlet, design of, 275–281

- inlet velocity limitations at eye, 272–273
  - kinetic energy at impeller, 298
  - mechanical arrangement, 488*f*
  - Mollier diagram for, 270*f*
  - overall efficiency, 503–504
  - performance of, 292–300
  - pressure ratio, 292–294
  - stage and velocity diagrams, 268*f*
  - thermodynamic analysis of, 269–272
  - volute, 268, 300
  - Centrifugal pump
    - head increase of, 290–292
    - hydraulic efficiency of, 290
    - impellers, 284, 290
    - volute, 300
  - Centripetal turbine. *See* 90° Inward-flow radial (IFR) turbines
  - CFD. *See* Computational fluid dynamics (CFD)
  - Choked flow, 21
  - Coefficient
    - contraction, 70
    - drag, 82–83, 205–206, 445–446
    - energy loss, 78
    - enthalpy loss, 333–334
    - flow, 48, 122, 126, 146*f*, 182, 403
    - lift, 82–83, 205–206, 208–212, 445–446
    - nozzle loss, 333–334
    - power, 436–437, 461*f*
    - pressure rise, 78
    - profile loss, 97, 98*f*
    - rotor loss, 334
    - stagnation pressure loss, 77, 79
    - total pressure loss, 77
  - Compressible flow
    - actuator disc theory for, 241–242
    - diffuser performance in, 305–308
    - equation, 502
    - through fixed blade row, 229
    - for perfect gas, 507*i*, 513*r*
  - Compressible fluid analysis, 44–48
  - Compressible gas flow relations, 18–21
  - Compressible specific speed, 60–61
  - Compression process, 27–29
  - Compressor, 267. *See also* Centrifugal compressor
    - blade profiles, 73–74
    - high speed, 48–49
  - Compressor cascade, 84–95
    - and blade notation, 73*f*
    - choking of, 95
    - Lieblein's correlation, 84–85
    - Mach number effect, 92–94
    - Mollier diagrams for, 78
    - performance characteristics, 84–95
    - pitch–chord ratio, 85
    - velocity distribution, 85*f*
    - wake momentum thickness ratio, 89, 91*f*
    - wind tunnels, 70*f*
  - Compressor stage, 218–221
    - high Mach number, 195–198
    - mean-line analysis, 170–171
    - off-design performance, 187–188, 232–233
    - reaction, 182–183
    - stage loading, 181–182
    - stage loss relationships and efficiency, 173–176
    - thermodynamics of, 172–173
    - velocity diagrams of, 172*f*
  - Computational fluid dynamics (CFD), 129
    - application in hydraulic turbines design, 398
    - methods, 69
  - Conical diffuser, 271*f*, 308–309, 308*f*
  - Constant specific mass flow, 230–232
  - Contraction coefficient, 70
  - Cordier diagram, 56–59
  - Correlation
    - Ainley and Mathieson, 96–98
    - Lieblein, 84–85
    - Soderberg, 99–101, 140
  - Critical point, 18
  - Cut-in wind speed, 427
  - Cut-out wind speed, 427
- ## D
- Darcy's equation, 371
  - Darrieus turbine, 423
  - De Haller number, 85–86
  - Deflection of fluid, 86–87
  - Design
    - of centrifugal compressor inlet, 275–281
    - of pump inlet, 273–275
  - Deviation of fluid, 86–87
  - Diffuser, 268, 271–272, 300–305
    - conical, 271*f*, 308–309, 308*f*
    - design calculation, 308–309
    - efficiency, 305–306
    - performance parameters, 305–309
    - radial, 302, 302*f*, 303*f*
    - two-dimensional, 271*f*, 304*f*
    - vaned, 303–305
    - vaneless, 301–302
  - Diffusion factor (DF), 85
    - local, 84–85
  - Diffusion in turbine blades, 141–143
  - Dimensional analysis, 39–40
  - Direct problem, radial equilibrium equation for, 227–229

Drag coefficient, 82–83, 205–206, 445–446  
 Drag forces, 81–82  
 Dryness fraction, 18  
 Ducted fans, 204–212  
 Dunham and Came improvements, 96–97

## E

Efficiency  
 of compressors and pumps, 26–27  
 correlation, 143–146  
 design point, 146–150  
 diffuser, 305–306  
 hydraulic turbines, 25, 363–365, 381f  
 isentropic, 22, 26  
 mechanical, 22  
 nominal design point, 326–330  
 optimum, IFR turbine, 334–340  
 overall, 22  
 reaction effect on, 140–141  
 size effect on turbomachine, 389–391  
 small stage/polytropic, 27–33  
 steam and gas turbines, 23–25  
 turbine, 22, 127–133  
 turbine polytropic, 31  
 Endwall profiling, 252  
 Energy loss coefficient, 78  
 Energy transfer coefficient, 41  
 Enthalpy loss coefficient, 333–334  
 Entropy, 11–13  
 Environmental considerations for wind turbine  
 acoustic emissions, 480  
 visual intrusion, 479–480  
 Environmental matters for wind turbine, 478–480  
 Equation of continuity, 6–7  
 Euler method, 110–111  
 Euler's equation  
 pump, 10  
 turbine, 10, 381  
 work, 10–11  
 Exhaust energy factor, 349, 350f

**F**

Fans, 265, 267–269  
 axial-flow, 204, 204f  
 ducted, 204–212  
 lift coefficient of, 208–212  
 First law of thermodynamics, 7–8  
 Flow angle, 230–231  
 Flow coefficient, 47–48, 122, 126, 146f, 182, 403  
 Flow velocities, 3f, 4  
 Fluid deviation, 86–87

Fluids, thermodynamic properties of, 14–18  
 Forced vortex design, 222

## Forces

drag, 81–82  
 lift, 81–82  
 Francis turbine, 2f, 319, 377–385  
 balding, sectional sketch of, 379f  
 basic equations, 381–384  
 capacity of, 365–366  
 cavitation in, 391, 392f  
 design point efficiency of, 364f  
 hydraulic efficiency of, 381f  
 runner of, 379f  
 velocity triangles for, 380f  
 vertical shaft, 378f, 382f  
 volute, 377–385

Free-vortex flow, 218, 229, 385–386  
 Free-vortex turbine stage, 233–235

## G

Gas turbines, cooling system for, 155–157  
 Gaussian probability density distribution, 427, 428f

## H

Head coefficient, 41  
 High-speed machines  
 performance characteristics for, 48–52  
 Horizontal axis wind turbine (HAWT), 423  
 aerofoils for, 466–467, 468f  
 blade section criteria, 466–467  
 energy storage, 429  
 tower height, 426–427  
 HP turbine  
 nozzle guide vane cooling system, 158f  
 rotor blade cooling system, 157f  
 Hub–tip radius ratios, 72  
 Hydraulic efficiency, 22, 26  
 of centrifugal pump, 290  
 Hydraulic turbines, 25, 319, 361–362. *See also* Francis turbine, Kaplan turbine; Pelton turbine  
 application ranges of, 365f  
 cavitation in, 391–397  
 design of, CFD application to, 398  
 flow regimes for maximum efficiency of, 363–365  
 history of, 363  
 operating ranges of, 364r  
 radial-inflow, 363  
 Hydropower, 361  
 harnessed and harnessable potential of, distribution of, 362r  
 Hydropower plants, features of, 362, 363r

## I

- Ideal gases, 14–15
- IFR turbines. *See* Inward-flow radial (IFR) turbines
- Impellers
  - centrifugal compressor, 268–271, 298, 310
  - centrifugal pump, 284, 290
  - efficiency, 499
  - exit, design of, 499–500
  - head correction factors for, 292*f*
  - inlet, design of, 498–499
  - kinetic energy at, 298
  - Mach number at exit, 295–297, 297*f*
  - prewhirl vanes at, 279–281
  - stresses in, 294
  - total-to-total efficiency of, 298
- Impulse blading, 97, 98*f*
- Impulse turbine stage, 137*f*
- Incidence loss, 333
- Incompressible cascade analysis, 89–91
- Incompressible flow
  - parallel-walled radial diffuser in, 302, 303*f*
- Incompressible fluid analysis, 40–42
- Indirect problem, radial equilibrium equation
  - for, 218–227
    - compressor stage, 218–221
    - first power stage design, 223–227
    - forced vortex, 222
    - free-vortex flow, 218
    - mixed vortex design, 223
    - whirl distribution, 222
- Inequality of Clausius, 11–12
- Inviscid methods, 112
- Inward-flow radial (IFR) turbines, 319, 487
  - 90 degree type. *See* 90° Inward-flow radial (IFR) turbines
  - cantilever, 320–321
  - efficiency levels of, 344*f*
  - optimum efficiency, 334–340
  - types of, 320–322
- 90° Inward-flow radial (IFR) turbines, 321–322
  - cooling of, 354–359
  - loss coefficients in, 333
  - Mollier diagram, 323*f*
  - optimum design selection of, 351–352
  - optimum efficiency, 334–340
  - specific speed, significance and
    - application, 348–351
  - specific speed function, 350*f*
  - thermodynamics of, 322–324
- Isentropic efficiency, 22
- Isentropic process, 12, 26
- Isentropic temperature ratio, 488

## K

- Kaplan turbine, 2*f*, 363, 385–389
  - basic equations, 386–389
  - cavitation in, 393*f*
  - design point efficiencies of, 364*f*
  - flow angles for, 389*f*
  - hydraulic efficiency of, 381*f*
  - runner of, 385–386
  - velocity diagrams of, 387*f*
- Kinetic power, of wind turbines, 428
- Kutta–Joukowski theorem, 83

## L

- Leading edge spike, 87
- Leakage flows, 250
- Leakage paths, seals, and gaps, 252–254
- Lean, 252
- Lieblein's correlation, 84–85
- Lift coefficient, 82–83, 205–206, 445–446
  - of fan aerofoil, 208–212
- Lift forces, 81–82
- Lifting surface, prescribed wake theory (LSWT), 476
- Ljungström steam turbine, 319, 320*f*
- Local diffusion factor, 84–85
- Loss bucket, 95
- Loss coefficients in 90° IFR turbines, 333
- Loss loop, 95
- Low-speed machines
  - performance characteristics for, 42–44

## M

- Mach number, 18, 230–231, 501
  - blade, 293, 295
  - compressor stage, 195–198
  - effects of, 92–95
    - at impeller exit, 295–297, 297*f*
    - radial flow gas turbines, 330–331
- Mach number effects on loss, 101–102
- Manometric head, 290
- Matrix through-flow method, 243
- Mean radius velocity triangles, 489–490
- Mean velocity, 81
- Mean-value rule, 239
- Mechanical efficiency, 22
- Meridional velocity, 3–4
- Mixed flow turbomachines, 1, 2*f*
- Mixed-flow turbomachinery, 58–60
- Mollier chart, for steam, 521*f*
- Mollier diagram, 17
  - 90° IFR turbine, 323*f*
  - for axial compressor stage, 173*f*

## I

- Ideal gases, 14–15
- IFR turbines. *See* Inward-flow radial (IFR) turbines
- Impellers
  - centrifugal compressor, 268–271, 298, 310
  - centrifugal pump, 284, 290
  - efficiency, 499
  - exit, design of, 499–500
  - head correction factors for, 292*f*
  - inlet, design of, 498–499
  - kinetic energy at, 298
  - Mach number at exit, 295–297, 297*f*
  - prewhirl vanes at, 279–281
  - stresses in, 294
  - total-to-total efficiency of, 298
- Impulse blading, 97, 98*f*
- Impulse turbine stage, 137*f*
- Incidence loss, 333
- Incompressible cascade analysis, 89–91
- Incompressible flow
  - parallel-walled radial diffuser in, 302, 303*f*
- Incompressible fluid analysis, 40–42
- Indirect problem, radial equilibrium equation
  - for, 218–227
    - compressor stage, 218–221
    - first power stage design, 223–227
    - forced vortex, 222
    - free-vortex flow, 218
    - mixed vortex design, 223
    - whirl distribution, 222
- Inequality of Clausius, 11–12
- Inviscid methods, 112
- Inward-flow radial (IFR) turbines, 319, 487
  - 90 degree type. *See* 90° Inward-flow radial (IFR) turbines
  - cantilever, 320–321
  - efficiency levels of, 344*f*
  - optimum efficiency, 334–340
  - types of, 320–322
- 90° Inward-flow radial (IFR) turbines, 321–322
  - cooling of, 354–359
  - loss coefficients in, 333
  - Mollier diagram, 323*f*
  - optimum design selection of, 351–352
  - optimum efficiency, 334–340
  - specific speed, significance and application, 348–351
  - specific speed function, 350*f*
  - thermodynamics of, 322–324
- Isentropic efficiency, 22
- Isentropic process, 12, 26
- Isentropic temperature ratio, 488

## K

- Kaplan turbine, 2*f*, 363, 385–389
  - basic equations, 386–389
  - cavitation in, 393*f*
  - design point efficiencies of, 364*f*
  - flow angles for, 389*f*
  - hydraulic efficiency of, 381*f*
  - runner of, 385–386
  - velocity diagrams of, 387*f*
- Kinetic power, of wind turbines, 428
- Kutta–Joukowski theorem, 83

## L

- Leading edge spike, 87
- Leakage flows, 250
- Leakage paths, seals, and gaps, 252–254
- Lean, 252
- Lieblein's correlation, 84–85
- Lift coefficient, 82–83, 205–206, 445–446
  - of fan aerofoil, 208–212
- Lift forces, 81–82
- Lifting surface, prescribed wake theory (LSWT), 476
- Ljungström steam turbine, 319, 320*f*
- Local diffusion factor, 84–85
- Loss bucket, 95
- Loss coefficients in 90° IFR turbines, 333
- Loss loop, 95
- Low-speed machines
  - performance characteristics for, 42–44

## M

- Mach number, 18, 230–231, 501
  - blade, 293, 295
  - compressor stage, 195–198
  - effects of, 92–95
    - at impeller exit, 295–297, 297*f*
    - radial flow gas turbines, 330–331
  - Mach number effects on loss, 101–102
- Manometric head, 290
- Matrix through-flow method, 243
- Mean radius velocity triangles, 489–490
- Mean velocity, 81
- Mean-value rule, 239
- Mechanical efficiency, 22
- Meridional velocity, 3–4
- Mixed flow turbomachines, 1, 2*f*
- Mixed-flow turbomachinery, 58–60
- Mollier chart, for steam, 521*f*
- Mollier diagram, 17
  - 90° IFR turbine, 323*f*
  - for axial compressor stage, 173*f*

**Mollier diagram** (*Continued*)

- for axial turbine stage, 125*f*
- for centrifugal compressor stage, 270*f*
- compression process, 27–29
- compressor blade cascade, 78*f*
- compressors and pumps, 26
- for diffuser flow, 305*f*
- for fifty percent reaction turbine stage, 137*f*
- for impulse turbine stage, 123–124
- reheat factor, 31–33, 32*f*
- steam and gas turbines, 23–25
- turbine blade cascade, 78*f*
- for zero reaction turbine stage, 136*f*

**Momentum**

- equation, 9–11
- moment of, 9

**Multiple blade row steady computations, 255–256****Multi-stage compressor, 188–195**

- annulus wall boundary layers, 194–195
- off-design operation, 190–193
- overall pressure ratio and efficiency, 188–190
- pressure ratio of, 188–190
- stage matching, 190–193
- stage stacking, 193
- ultimate steady flow, 194–195

**Multistage turbines, 124–125**

- flow characteristics, 160–166

**N****National Advisory Committee for Aeronautics (NACA), 73–74****Navier–Stokes method, 110–112****Neap tide, 409, 410*f*****Net positive suction head (NPSH), 63, 273, 391–392****Newton's second law of motion, 9****Nozzle loss coefficients, 333–334****NPSH. See Net positive suction head (NPSH)****O****Off-design performance of compressor, 187–188****Optimum design**

- of 90° IFR turbines, 337, 351–352
- of centrifugal compressor inlet, 275–281

**Optimum efficiency, IFR turbine, 334–340****Optimum space–chord ratio, 102****Overall efficiency, 22****P****Panel (or vortex) method, 109****Peak and post-peak power predictions, 477–478****Pelton turbine, 61, 61*f*, 363, 366–377****design point efficiencies of, 364*f*****energy losses in, 371–372****hydraulic efficiency of, 381*f*****hydroelectric scheme, 369, 370*f*****jet impinging on bucket, 368*f*****optimum jet diameter, 372–375****overall efficiency of, 374, 375*f*****runner of, 367*f*****six-jet vertical shaft, 368*f*****sizing the penstock, 371****speed control of, 369–371****surge tank, 369****water hammer, 371****Pelton wheel, 2*f*****Perfect gases, 15–17****Performance prediction codes, wind turbine, 475–478****Peripheral velocity factor (PVF), 395–396****Pitch–chord ratio, 85****Power coefficient, 436–437, 461*f*****at optimum conditions, 463*t*****Prandtl's tip correction factor, 453–455****Prescribed velocity distribution (PVD) method, 73****Pressure loss coefficient****stagnation, 77, 79****total, 77****Pressure ratio of multi-stage compressor, 188–190****Pressure rise coefficient, 78****Profile loss coefficient, 97****Pump, 267–269. See also Centrifugal pump****inlet, design of, 273–275****radial-flow, 269*f*****Q****Quality/dryness fraction, 18****Quasi-three-dimensional (Q3D) methods, 108****R****Radial diffuser, 302, 302*f*, 303*f*****Radial equilibrium, 215****direct problem, 227–229****equation, 215–217, 227****fluid element in, 215–217****indirect problem, 218–227****theory of, 215–217****Radial flow gas turbines, 319–320****basic design of rotor, 324–326****cantilever type, 320–321****clearance and windage losses, 352–354****cooling of, 354–359****criterion for number of vanes, 342, 343*f***

Francis type, 319  
 incidence loss, 333  
 IFR type. *See* Inward-flow radial (IFR) turbines  
 Ljungström steam type, 319, 320f  
 mach number relations, 330–331  
 nominal design point efficiency, 326–330  
 nozzle loss coefficients, 333–334  
 optimum design selection, 351–352  
 optimum efficiency considerations, 334–340  
 rotor loss coefficients, 334  
 scroll and stator blades, 331–334  
 spouting velocity, 325–326  
 stator loss models, 332–333  
 vaneless space and vane solidity, 333  
 velocity triangles, 321f, 322  
 Radial flow turbomachine, 1  
 Rayleigh distribution, 432, 433f  
 Reaction, turbine stage, 126  
   fifty percent, 136–139  
   zero value, 136, 148, 149f  
 Reaction turbine, 377  
 Reheat factor, 31–33  
 Relative eddy, 282  
 Relative roughness, 42  
 Relative velocity, 4, 11  
 Reynolds number, 41–42  
 Reynolds number correction, 99  
 Right turbine, selecting, 396–397  
 Rotating stall in compressor, 198  
 Rothalpy, 11, 124  
 Rotor, 176–180  
   compressible case, 176–177  
   incompressible case, 178–180  
 Rotor blade configurations, 458–465  
   blade variation effect, 458  
   optimum design criteria, 460–465  
   planform, 458  
   tip-speed ratio effect, 459–460  
 Rotor design, 324–326, 343–348  
   nominal, 324–325  
   Whitfield, 337–340  
 Rotor loss coefficients, 334  
 Roughness ratio, 42

## S

Saturated liquid, 17–18  
 Saturated vapor, 17–18  
 Saturation curve, 17–18  
 Scroll. *See* Volute  
 SeaGen tidal turbine, 362, 411–417  
 Second law of thermodynamics, 11–13  
 Secondary flows, 246–250

  passage vortex, 248  
   vorticity, 246–248  
 Semi-perfect gas, 15  
 Settling-rate rule, 239  
 Shock loss, 333  
 SI units, British and American units conversion  
   to, 419r–486r  
 Sign convention, 4  
 Single-passage computations, 255  
 Slip factor, 281–285  
   Busemann, 284  
   correlations, 282–285  
   Stanitz, 284–285  
   Stodola, 283  
   unified correlation for, 286–290  
   Wiesner, 285  
 Soderberg's correlation, 99–101, 140  
 Solid-body rotation, 222. *See also* Forced  
   vortex design  
 Space-chord ratio, 72, 494  
 Specific diameter, 53–61  
 Specific speed, 53–61, 394–395  
   compressible, 60–61  
   efficiency for turbines, 350f  
   significance and application of, 348–351  
 Spouting velocity, 325–326  
 Spring tide, 409, 410f  
 Stage loading, 48, 123, 126, 146f, 181–182  
 Stage matching, 190–193  
 Stage stacking, 193  
 Stagger angle, 72  
 Stagnation enthalpy, 8, 18–19  
 Stagnation pressure loss coefficient, 77, 79  
 Stall and surge in compressor, 198–203  
 Stanitz's expression for slip velocity, 284–285  
 Stator loss models, 332–333  
 Steady flow  
   energy equation, 8  
   moment of momentum, 9  
   momentum equation, 9  
 Steam, 17–18  
   and gas turbines, 23–25  
 Steam turbines, 119, 131–133  
   low pressure, 120f  
 Streamline curvature method, 243–245  
 Streamtube thickness variation, 76–77  
 Stresses in turbine rotor blades, 150–155  
   centrifugal, 151–155  
 Suction specific speed, 394–395  
 Superheat of steam, degree of, 18  
 Surge margin, 48–49  
 Sweep, 251–252

## T

- Tangential flow induction factor, 442
- Tangential velocity distribution, 222
- Thermodynamic properties of fluids, 14–18
  - ideal gases, 14–15
  - perfect gases, 16–17
  - steam, 17–18
- Thoma coefficient, 391–392, 394–395
- 3D computational fluid dynamics (3D CFD)
  - application in axial turbomachines, 254–263
  - multiple blade row steady computations, 255–256
  - single-passage computations, 255
  - unsteady computations, 257
- 3D design, 251–254
  - endwall profiling, 252
  - leakage paths, seals, and gaps, 252–254
  - lean, 252
  - sweep, 251–252
- Three-dimensional flows in axial turbomachines, 215
- Throat, 21
- Through-flow problem
  - computer-aided methods of solving, 242–245
  - techniques for solving, 243
- Tidal power, 362, 409–417. *See also* SeaGen tidal turbine
  - categories of, 410
- Tidal stream generators, 410–411
- Tides
  - neap, 409, 410f
  - range, 409
  - spring, 409, 410f
- Time-marching method, 243
- Tip-speed ratio, 448, 459–460
- Total-to-static efficiency, 24, 326, 351–352
  - effect of reaction on, 140–141
  - of stage with axial velocity at exit, 148–150, 149f
- Total-to-total efficiency, 23
  - of fifty percent reaction turbine stage, 146–147
  - of impeller, 298
  - of turbine stage, 127
  - of zero reaction turbine stage, 148, 149f
- Triple point for water, 18
- Turbine cascade (two-dimensional), 95–108
  - Ainley and Mathieson correlation, 96–98
  - Dunham and Came improvements, 96–97
  - flow exit angle, 105–106
  - flow outlet angles, 97–98
  - limit load, 106–108
  - Mach number effects on loss, 101–102
  - optimum space to chord ratio, 102–103
  - Reynolds number correction, 99
  - Soderberg's correlation, 99–101
  - turbine limit load, 106–108
  - turbine loss correlations, 95–96
  - Zweifel criterion, 102–105
- Turbine efficiency, 22
- Turbine polytropic efficiency, 31
- Turbines
  - axial-flow. *See* Axial-flow turbines
  - Francis. *See* Francis turbine
  - free-vortex stage, 233–235
  - high speed, 49–52
  - hydraulic. *See* Hydraulic turbines
  - Kaplan. *See* Kaplan turbine
  - off-design performance of stage, 232–233
  - Pelton. *See* Pelton turbine
  - radial flow gas. *See* Radial flow gas turbines
  - reaction, 377
  - Wells. *See* Wells turbine
  - wind. *See* Wind turbine
- Turbochargers, 487
  - advantages, 487
  - efficiency, size effect on, 389–391
  - types, 487
- Turbomachines
  - categories of, 1
  - as control volume, 9, 10f, 40f
  - coordinate system, 2–6
  - definition of, 1–2
  - flow unsteadiness, 33–36
  - performance characteristics of, 42–44
- Turbomachines, axial
  - blade rows in, 239
  - endwall profiling, 252
  - leakage paths, seals, and gaps, 252–254
  - lean, 252
  - solving through-flow problem in, 242–245
  - sweep, 251–252
  - 3D design of, 251–254
- Two-dimensional cascades. *See* Cascades, two-dimensional

## U

- Unsteadiness paradox, 33
- Unsteady 3D computations, 257

## V

- Vaned diffuser, 303–305, 503
- Vaneless diffuser, 301–302
  - space, flow in, 500–503
- Vapour pressure, 62–63
- Velocity, spouting, 325–326
- Velocity diagrams for axial flow compressor stage, 5–6
- Velocity triangles for root, mean and tip radii, 493f, 494
- Vertical axis wind turbine (VAWT), 423



- Volute, 301–302, 503
  - centrifugal compressor, 268, 300, 301f
  - centrifugal pump, 300, 301f
- Vorticity, secondary, 246–248

## W

- Wake momentum thickness ratio, 89, 91f
- Wave power, 362. *See also* Wells turbine
- Weibull Distribution, 432–433
- Wells turbine, 362, 398–399, 399f
  - blade of, velocity and force vectors acting on, 401f
  - blade solidity effect on, 403–404
  - characteristics under steady flow conditions, 406
  - design and performance variables, 402–405
  - flow coefficient, effect on, 403
  - hub–tip ratio, effect on, 404
  - operating principles, 400
  - and oscillating water column, 398
  - self pitch-controlled blades, 405–408
  - starting behaviour of, 405, 405f
  - two-dimensional flow analysis, 400–402
- Wet steam, 17
- Whirl distribution, 222
- White noise, 62
- Whitfield's design of rotor, 337–340
- Wind data
  - basic equations, 431–432
  - statistical analysis of, 431–433
- Wind energy
  - availability, 420
  - characteristics, 420–422
  - resource estimation, 420–422
- Wind shear, 426–427
- Wind speed probability density function, 427–428
- Wind speed probability distributions, 432–433
  - Rayleigh distribution, 432, 433f
  - Weibull distribution, 432–433
- Wind turbine, 419–422, 481
  - blade section criteria, 466–467
  - control methods, 469–473
  - cut-in wind speed, 427
  - cut-out wind speed, 427
  - environmental matters, 478–480
  - historical viewpoint, 422
  - idealized power output curve for, 428f
  - kinetic power, 428
  - maximum possible power production
    - of, 429–430
  - performance measurement of, 427–430
  - performance testing, 474
  - power coefficient of, 436–437
  - power output, 441
  - Prandtl's blade tip correction for, 453–455
  - prediction of power output, 427
  - rated output power, 428
  - rotor blade configuration, 458–465
  - size of, 481
  - solidity, 448
  - stall control, 471
  - types of, 422–427
- Windmills, 422

## Z

- Zero lift line of aerofoil, 208–212
- Zero reaction turbine stage, 136
  - Mollier diagram for, 136f
  - total-to-total efficiency of, 148, 149f
- Zweifel criterion, 102–105