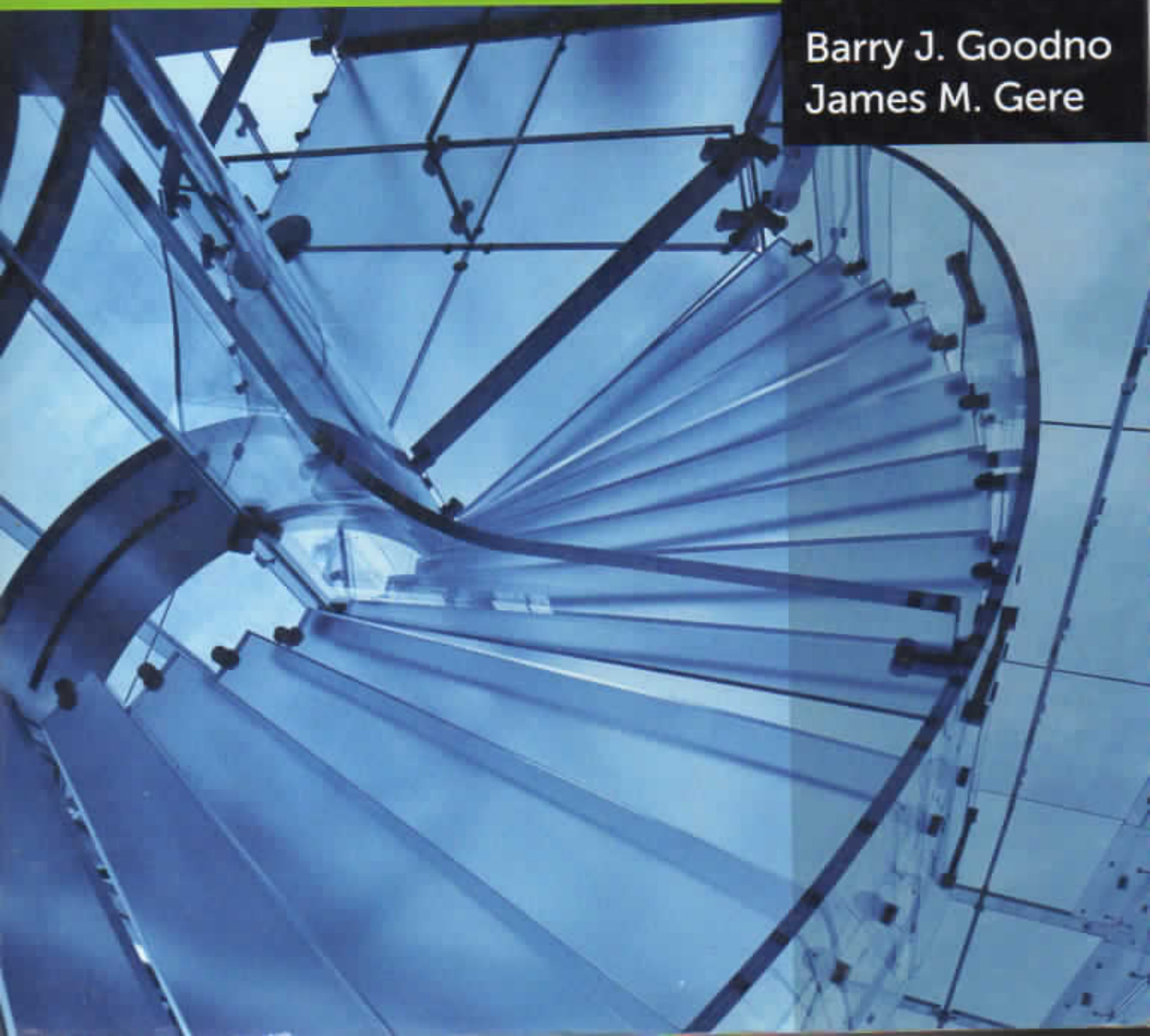
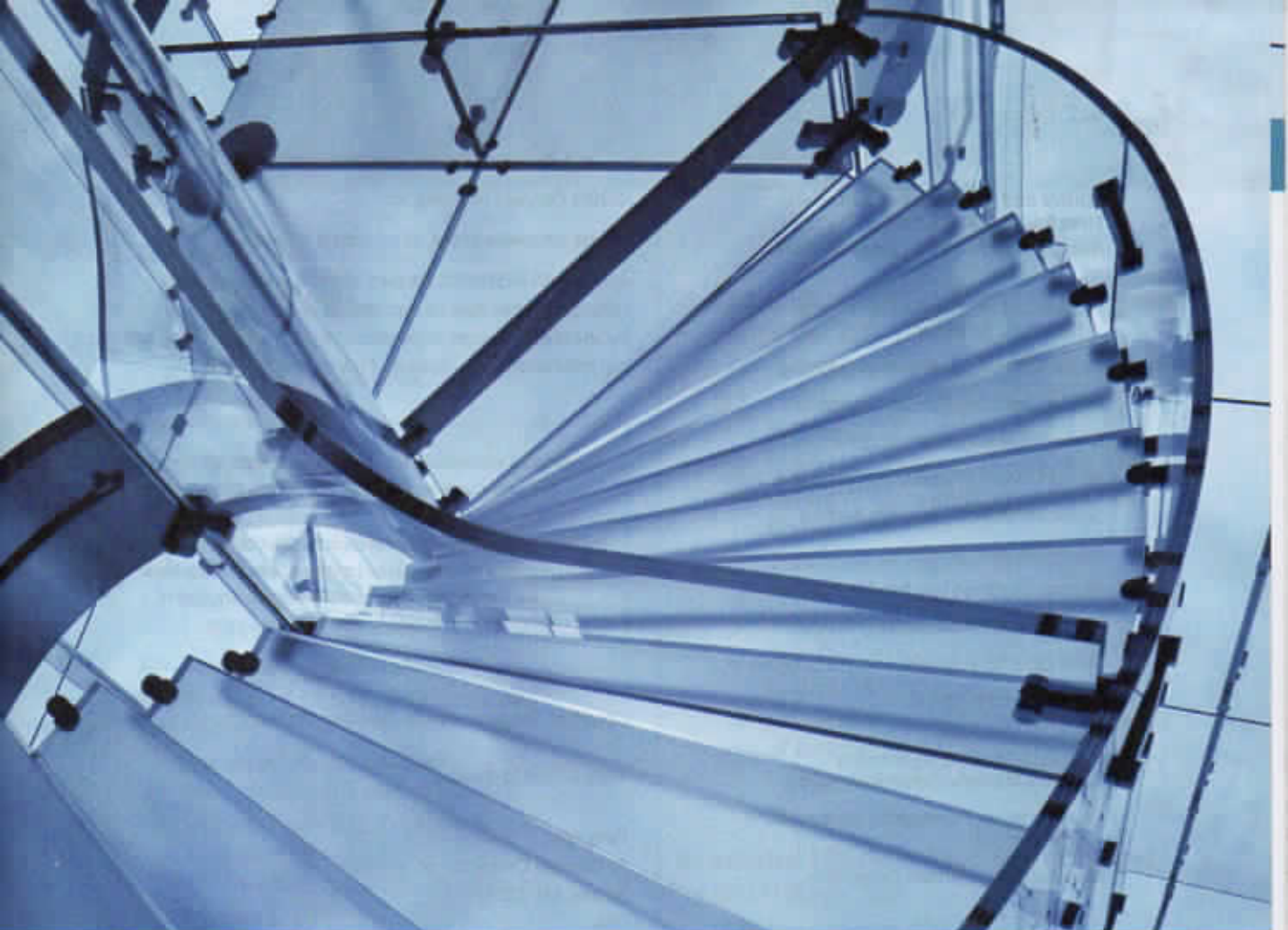


SI EDITION

STATICS AND MECHANICS OF MATERIALS

Barry J. Goodno
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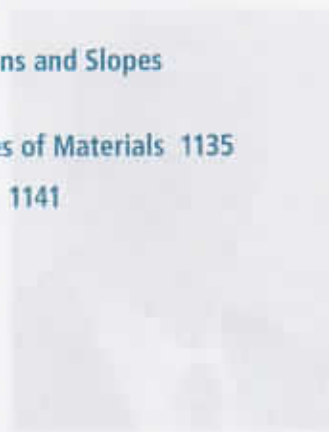


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